U.S. Army Coast. Eug. Res. G.TP 82-2

-HiBREN

Computer Algorithm to Calculate Longshore Energy Flux and Wave Direction from a Two Pressure Sensor Array

by

Todd L. Walton, Jr. and Robert G. Dean

TECHNICAL PAPER NO. 82-2

AUGUST 1982



Approved for public release; distribution unlimited.



U.S. ARMY, CORPS OF ENGINEERS COASTAL ENGINEERING RESEARCH CENTER

> Kingman Building Fort Belvoir, Va. 22060

Reprint or republication of any of this material shall give appropriate credit to the U.S. Army Coastal Engineering Research Center.

Limited free distribution within the United States of single copies of this publication has been made by this Center. Additional copies are available from:

> National Technical Information Service ATTN: Operations Division 5285 Port Royal Road Springfield, Virginia 22161

The findings in this report are not to be construed as an official Department of the Army position unless so designated by other authorized documents.



UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION	PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM		
1. REPORT NUMBER	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER		
TP 82-2				
4. TITLE (and Subtitie)		S. TYPE OF REPORT & PERIOD COVERED		
COMPUTER ALGORITHM TO CALCULATE LO	NGSHORE	Technical Paper		
PRESSURE SENSOR ARRAY		5. PERFORMING ORG. REPORT NUMBER		
7. AUTHOR(a)		8. CONTRACT OR GRANT NUMBER(8)		
Todd L. Walton, Jr. Robert G. Dean				
9. PERFORMING ORGANIZATION NAME AND ADDRESS	,	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS		
Department of the Army				
Coastal Engineering Research Cente Kingman Building, Fort Belvoir, Vi	r (CEREN-EV) rginia 22060	C31181		
11. CONTROLLING OFFICE NAME AND ADDRESS		12. REPORT DATE		
Department of the Army	-	August 1982		
Kingman Building, Fort Belvoir, Vi	rginia 22060	33		
14. MONITORING AGENCY NAME & ADDRESS(If differen	t from Controlling Office)	15. SECURITY CLASS. (of this report)		
		UNCLASSIFIED		
		15e. DECLASSIFICATION/DOWNGRADING SCHEDULE		
Approved for public release; distribution unlimited. 17. DISTRIBUTION STATEMENT (of the obstract entered in Block 20, 11 different from Report)				
18. SUPPLEMENTARY NOTES				
19. KEY WORDS (Continue on reverse side if necessary an	d identify by block number)			
Computer program Longshore energy flu	Wav x Wav	e gage array e spectra		
bediment transport				
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) A documented (FORTRAN IV) computer program is discussed as originally written for the CERC Longshore Sand Transport Research Program to analyze wave data collected at Channel Islands Harbor, California.				
The program performs the basic necessary to compute wave directio	analysis of two on and wave ener	wave gage pressure records gy at a given frequency and (continued)		

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)

SECURITY CLASSIFICATION OF THIS PAGE(When Date Entered)

computes the longshore energy flux used in sand transport for the entire energy spectrum of the wave record. This program uses linear wave theory for the wave transformation process and includes the assumption of straight and parallel bottom contours necessary for application of Snell's law of refraction.

The necessary steps in an analysis of wave data and sample outputs for some wave records from the Channel Islands wave gage pressure sensor pair are given. The program presently accepts data in the standard CERC magnetic-tape format where record lengths consist of 4,100 values.

PREFACE

This report provides coastal engineers with documentation necessary to compute the longshore energy flux used in sand transport rate calculation when random waves are present and synchronous data from two closely spaced pressure transducers exist. The documentation is based on a 3-year data collection effort and study of sand transport rates at Channel Islands Harbor, California. The computer program documented herein was used in wave data analysis for a two pressure sensor array installed in 30 feet of water at the site. The work was carried out under the U.S. Army Coastal Engineering Research Center's (CERC) Littoral Data Collection work unit, Shore Protection and Restoration Program, Coastal Engineering Area of Civil Works Research and Development.

This report was prepared by Dr. Todd L. Walton, Jr., Hydraulic Engineer, CERC, and Dr. Robert G. Dean, Department of Civil Engineering and College of Marine Studies, University of Delaware. Dr. Walton worked on the project under the general supervision of Dr. J.R. Weggel, Chief, Evaluation Branch, and Mr. N. Parker, Chief, Engineering Development Division.

Technical Director of CERC was Dr. Robert W. Whalin, P.E., upon publication of this report.

Comments on this publication are invited.

Approved for publication in accordance with Public Law 166, 79th Congress, approved 31 July 1945, as supplemented by Public Law 172, 88th Congress, approved 7 November 1963.

Colonel, Corps of Engineers Commander and Director

CONTENTS

	CONTREPCTON FACTORS II S CUSTOMARY TO METRIC (ST)	Page
	CONVERSION FROTORS, 0.5. COSTOMART TO METRIC (SI)	ر ،
	SYMBOLS AND DEFINITIONS	6
I	INTRODUCTION	. 7
II	METHODOLOGY. 1. Calculation of Wave Direction and Energy Spectrum at Wave Gages. 2. Transformation of Wave Spectrum to Breaker Line	7 8 12
III	MAIN PROGRAM DOCUMENTATION	13
IV	SUBROUTINE DOCUMENTATION. 1. FFT Subroutine. 2. HFC Subroutine. 3. SWITCH Subroutine. 4. WVLEN Subroutine. 5. BUF Subroutine.	22 22 26 27 27 27 28
V	SAMPLE OUTPUT.	29
	LITERATURE CITED	33

FIGURES

1	Definition sketch for two sensor array	10
2	Listing of main program	14
3	Listing of FFT subroutine	25
4	Listing of HFC subroutine	27
5	Listing of SWITCH subroutine	27
6	Listing of WVLEN subroutine	28
7	Listing of BUF subroutine	29
8	Three examples of output for wave gage pair at Channel Islands Harbor	30

U.S.	customary	units	of	measurement	used	in	this	report	can	be	converted	to
metri	ic (SI) uni	its as	fo	llows:								

Multiply	by	To obtain
inches	25.4	millimeters
	2.54	centimeters
square inches	6.452	square centimeters
cubic inches	16.39	cubic centimeters
feet	30.48	centimeters
	0.3048	meters
square feet	0.0929	square meters
cubic feet	0.0283	cubic meters
yards	0.9144	meters
square yards	0.836	square meters
cubic yards	0.7646	cubic meters
miles	1.6093	kilometers
square miles	259.0	hectares
knots	1.852	kilometers per hour
acres	0.4047	hectares
foot-pounds	1.3558	newton meters
millibars	1.0197×10^{-3}	kilograms per square centimeter
ounces	28.35	grams
pounds	453.6	grams
poundo	0.4536	kilograms
ton, long	1.0160	metric tons
ton, short	0.9072	metric tons
degrees (angle)	0.01745	radians
Fahrenheit degrees	5/9	Celsius degrees or Kelvins ¹

¹To obtain Celsius (C) temperature readings from Fahrenheit (F) readings, use formula: C = (5/9) (F -32).

To obtain Kelvin (K) readings, use formula: K = (5/9) (F - 32) + 273.15.

SYMBOLS AND DEFINITIONS

a _l ,b _l	Fourier series coefficients
В	distance from bottom to pressure sensors
Cg	wave celerity
C ₁₂	cospectrum value
d	total water depth
d _b	breaking wave depth
E	wave energy density
F	complex Fourier coefficient
fn	discrete frequency value
GB,GBP	ratio of rms breaking wave height to breaking wave depth
g	acceleration of gravity
н _ь	breaking wave height
i,j	counting indexes
Kz	dynamic pressure response factor
k	wave number
L	wavelength
٤	sensor spacing
m	index to account for gage number
N	total number of discrete data points
n	frequency number, argument of Fourier series coefficients
Pls	longshore energy flux at the surf line
P	pressure time-series values
P	dynamic pressure
Q ₁₂	quad-spectrum value
R	ratio of unwindowed energy density to windowed energy density
S ₁₂	complex cross-spectrum value
T	length of time series record
T _{HF}	high frequency cutoff period
W	weighting coefficient
z	water surface elevation
β	gage orientation angle
Y	specific weight of seawater
Θ	wave direction
∆d	average mean depth of water overlaying pressure sensors
Δf	frequency step
Δt	time step
ω	angular wave frequency

6

COMPUTER ALGORITHM TO CALCULATE LONGSHOKE ENERGY FLUX AND WAVE DIRECTION FROM A TWO PRESSURE SENSOR ARRAY

bu

Todd L. Walton, Jr. and Robert G. Dean

I. INTRODUCTION

The documented (FORTRAN IV programing language) computer program discussed in this report was originally written as part of the Coastal Engineering Research Center's (CERC) Longshore Sand Transport Research Program and was used in analysis of wave data collected at Channel Islands Harbor in conjunction with a study of sand transport at Channel Islands Harbor as discussed in Bruno, et al. (1981).

The program performs the basic analysis of two wave gage pressure records necessary to compute wave direction and wave energy at a given frequency and computes the longshore energy flux used in sand transport for the entire energy spectrum of the wave record. This program uses linear wave theory for the wave transformation process and includes the assumption of straight and parallel bottom contours necessary for application of Snell's law of refraction.

Necessary steps in the analysis of the wave data are presented in Sections II and III of this report. Subroutines are discussed and sample outputs for some wave records from the Channel Islands wave gage pressure sensor pair are given.

The program presently accepts data in the standard CERC magnetic-tape format where record lengths consist of 4,100 values. The first four values are the gage number and the date-time group, and the remaining 4,096 values are the pressures recorded in thousandths of a foot (head) of water at 0.25-second intervals. Should other input data be available, the program could easily be modified to accept the data by simple changes in the main program and in subroutines BUF and SWITCH.

Sample outputs have been presented for real wave data; some wave directional information cannot be obtained for all frequencies because the spectral information at some frequencies is ill-conditioned. The percent of energy for which this problem occurs is a small part of the energy (usually <3 percent) of the entire spectrum and is insignificant in energy-flux computations. Reasons for this feature are discussed later.

II. METHODOLOGY

Calculating the longshore energy flux at breaking required the following steps:

(1) Calculation of the frequency-by-frequency wave direction and energy at the location of the wave gages;

(2) determination of the breaking wave depth;

(3) transformation of the wave spectrum to the "breaker" line, including shoaling and refraction effects; and

(4) computation of $"{\rm P}_{\rm LS},$ " the longshore energy flux at the surfline.

Each of the steps is described below.

1. Calculation of Wave Direction and Energy Spectrum at Wave Gages.

As noted previously, each of the input time-series pressure records consists of 4,096 data points with a time increment of 0.25 second. To reduce computational costs, modified time series are formed for analysis by averaging four adjacent data points. These new time series contain 1,024 data points spaced at 1.0-second intervals. This increases the aliasing period from 0.5 to 2.0 seconds; however, this is justified as the pressure response factor for a water depth of 6 meters and a wave period of 2 seconds is approximately 0.005.

The time series are analyzed using a standard fast Fourier transform (FFT) program to determine the coefficients. For example, for pressure time series from gage 1

$$P_{1}(j) = \sum_{n=0}^{N-1} [a_{1}(n) - ib_{1}(n)] \exp\left(\frac{i2\pi n j}{N}\right)$$
(1)

in which $i = \sqrt{-1}$ and N is the total number of data points, $T/\Delta t = 1,024$, where T is the time series record length of 1,024 seconds, Δt the time increment of 1 second between samples, and j a discrete time t_j where $t_j = discrete$ time value = $j\Delta t$. The FFT coefficients are defined in terms of the pressure time series as

$$a_1(n) - ib_1(n) = \frac{1}{N} \sum_{j=0}^{N-1} P_1(j) \exp\left(-i \frac{2\pi n j}{N}\right)$$
 (2)

where the argument "n" of the Fourier coefficients a(n) and b(n) specifies the quantity to be a discrete function of wave frequency, f_n , where f_n , a discrete frequency value, is $n\Delta f$ (where $\Delta f = 1/T$) and the $a_1(0)$ term represents the mean value of the time-series pressure record for wave gage 1. Similar relationships exist for wave gage 2. In calculating the FFT coefficients, there are several options that may be employed in an attempt to reduce spectral leakage which arises due to representing an aperiodic time series by a periodic series. A large number of possible data windows (weighting functions for data) have been developed to reduce the adverse effects of spectral leakage (Harris, 1974). These can be expressed in the form of a weighting function w(j), such that the modified time series p'(j) is of the form

$$p'(j) = w(j) p(j)$$

in which p(j) is the digitized measured pressure value at time $t_j = j\Delta t$, and w(j) a weighting function. A characteristic of these weighting functions is that they are equal to unity at the midpoint of the time series and decrease to a lesser value near the two ends. In the present program, a "cosine bell" weighting function is used; however, through comparisons of $P_{g,s}$ with and without this function, it was established that the effect of the weighting function is expressed by

$$w(j) = \frac{1}{2} \left(1.0 - \cos \frac{2\pi j}{N} \right)$$
(3)

It is clear that the application of a weighting function will reduce the total energy in the record. This effect is partly compensated for by the following equation:

$$p''(j) = \sqrt{\frac{\langle p^2 \rangle}{\langle p^* \rangle}} p'(j)$$
(4)

thereby ensuring the same total energy in the altered and original time series, where $\langle p^2 \rangle$ is the mean square value of the original time series and $\langle p^{\,\prime 2} \rangle$ the mean square value of the weighted time series. It is the altered time series p"(j) that is subjected to FFT analysis. The primes will be dropped hereafter for convenience. The average mean depth of water overlying the pressure sensors, Δd , is obtained by averaging the m time series to obtain $a_m^{\,}(0)$. For two separate time series records, m = 1, 2 (wave gages 1 and 2),

$$\Delta d = 0.5 [a_1(0) + a_2(0)]$$
(5)

The total water depth, d, is the sum of Δd and the distance, B, of the pressure sensors above the bottom (in later examples $B \simeq 0.76$ meter).

Each FFT pressure coefficient is transformed to a water surface displacement coefficient by the following linear wave theory relationship discussed in the Shore Protection Manual (SPM) (see Ch. 2, U.S. Army, Corps of Engineers, Coastal Engineering Research Center, 1977):

water surface coefficients

dynamic pressure coefficients

$$[a_{m}(n), b_{m}(n)]_{\eta} = \frac{1}{\gamma K_{z}(n)} [a_{m}(n), b_{m}(n)]_{p}$$
(6)

in which the subscripts η and p denote water surface and dynamic pressure coefficients, respectively. The factor

$$K_{z}(n) = \frac{\cosh k(n) B}{\cosh k(n) d}$$
(7)

where γ is the specific weight of fluid (seawater) and is included when pressure coefficients are in normal units of pressure (i.e., N/M² or equivalent). In equation (7), B represents the distance of the pressure sensors above the bottom and k(n) is the wave number associated with the angular frequency, $\omega(n) = (2\pi n\Delta f)$, as obtained from the linear wave theory dispersion relationship

$$\omega(n)^2 = gk(n) \tanh k(n) d \tag{8}$$

One of the disadvantages of measuring waves with near-bottom pressure sensors is evident by examining equations (6) and (7). For the higher frequencies (shorter wave periods) $K_z(n)$ is very small which means that the higher frequency waves result in very small pressure fluctuations near the sea floor. Thus, to avoid contaminating the calculated water surface displacements, it is

usually necessary to apply a high frequency cutoff, above which the pressure contributions are discarded. The proper selection of this high frequency cutoff depends on the signal to noise characteristics of the pressure sensor and the signal conditioning system. In the present program, the high frequency cutoff was established at a wave period of 3.0 seconds. Wave gage analyses by Thompson (1980) have shown that a 3.0-second high frequency spectral cutoff value provides reasonable estimates of total wave energy at west coast (U.S.) locations.

Denoting hereafter the FFT coefficients for the water surface as a(n) and b(n), it is noted that the coefficients have the following properties:

$$\langle n^2 \rangle = \sum_{n=1}^{N-1} [a^2(n) + b^2(n)]$$
 (9)

$$a\left(\frac{N}{2}+n\right) = a\left(\frac{N}{2}-n\right) \tag{10}$$

$$b\left(\frac{N}{2}+n\right) = -b\left(\frac{N}{2}-n\right)$$
(11)

and thus

$$\langle \eta^2 \rangle = 2 \sum_{n=1}^{N/2} [a^2(n) + b^2(n)]$$
 (12)

Thus, the total (kinetic and potential) energy E(n) associated with a particular wave frequency component, n, is

$$E(n) = 2\gamma[a^2(n) + b^2(n)]$$
(13)

Now consider two wave or pressure sensors located at (x_1, y_1) and (x_2, y_2) (see Fig. 1). The results will be developed considering discrete frequencies.



Figure 1. Definition sketch for two sensor array.

The water surface displacement consistent with the assumption of one direction per frequency is

$$n(x, y, j) = \sum_{n=0}^{N-1} F(n) \exp \{i[n\omega_1 t - k_x(n) x - k_y(n) y]\}$$

$$= \sum_{n=0}^{N-1} [a(n) - ib(n)] \exp\left(\frac{i2\pi nj}{N}\right)$$
(14)

where ω_1 is the primary analysis frequency (= $2\pi/\text{record}$ length = $2\pi/\text{T}$ = $2\pi\Delta f$), and $\Theta(n)$ the direction of wave propagation at frequency $\omega(n) = n\omega_1$. The wave number components, $k_{\chi}(n)$ and $k_{y}(n)$, are expressed in terms of the wave number, k(n), and wave direction, $\Theta(n)$, as

$$k_{v}(n) = k(n) \cos \Theta(n)$$
(15)

$$k_{v}(n) = k(n) \sin \Theta(n)$$
(16)

The cross spectrum, $S_{12}(n)$, of the two measured water surface displacements (or dynamic pressures) is given by

$$S_{12}(n) = |F(n)|^2 \{ \exp -i [k(n) \cos \Theta(n)(x_2 - x_1) + k(n) \sin \Theta(n)(y_2 - y_1)] \}$$
(17)

Denoting the separation distance and angle as ℓ and β , respectively, the cross spectrum can be expressed as (see Fig. 1)

$$S_{12}(n) = |F(n)|^2 \{\cos [k(n) l \cos (\theta(n) - \beta)] - i \sin [k(n) l \cos (\theta(n) - \beta)] \}$$

= cospectrum (n) - i quad-spectrum (n) (18)
= C_{12}(n) - iQ_{12}(n)

Thus, from equation (18), the wave direction $\Theta(n)$ associated with each wave frequency can be expressed as

$$\Theta(n) = \beta \neq \cos^{-1} \left\{ \frac{1}{k(n) \ \ell} \tan^{-1} \left[\frac{Q_{12}(n)}{C_{12}(n)} \right] \right\}$$
(19)

The above relationship has two roots, one of which must be selected based on physical considerations of the most likely direction of wave propagation. In the present case, assuming no wave reflection from the beach, the ambiguity in wave direction is ruled out; for wave sensors nearly parallel to the beach, the minus sign in equation (19) is appropriate.

There are two conditions for which it was not possible to calculate the wave directions $\Theta(n)$. These include poorly conditioned wave data, presumably due to spectral leakage, and spatial aliasing due to large separation distance between the two gages. If the data are poorly conditioned for determining wave direction, the absolute value of the quantity within the brackets $\{-\}$ in equation (19) may exceed unity, a physically impossible condition since the extreme values of the cosine function are ±1. This tends to occur for the extremely long waves for which the energy is small and the value of k(n) is also small, the latter tending to result in large values of the bracketed quantity. The percentage of energy for which this condition occurred in the analysis of one year's wave data collected at Channel Islands Harbor was relatively small, averaging 2 to 3 percent with a maximum of approximately 10 percent. The second condition is related to spatial aliasing and requires that one-half the wavelength be equal to or greater than the projection of the wave gage separation distance in the direction of wave propagation. Referring to Figure 1.

$$L > 2\ell \left\{ \cos[\Theta(n) - \beta] \right\}_{max}$$
(20)

which indicates that for the least adverse effects of spatial aliasing, the gages should be on an alinement parallel to the dominant orientation of the wave crests. As will be discussed later, in calculating P_{ls} an attempt was made to account for this effect of aliasing by augmenting the calculated values, illustrated as follows by

$$(P_{ls})_{cm} = (P_{ls})_{c} \frac{E_{TOT}}{E}$$
(21)

in which the subscripts c and cm indicate calculated and calculated modified, respectively. $E_{\rm TOT}$ and E represent the total wave energy values and the wave energy not affected by spatial aliasing or poorly conditioned wave data, respectively. The total wave energy is that energy in the wave spectrum below the high frequency spectral cutoff value.

2. Transformation of Wave Spectrum to Breaker Line.

At this stage, the wave energy and wave direction in the vicinity of the gages are determined. These values are then transformed to the breaker line accounting for wave refraction and shoaling.

To determine the wave breaking depth, the onshore-directed energy flux is calculated in accordance with the expression (based on Snell's law of refraction) and equated to an equivalent expressed in terms of wave characteristics at breaking.

Onshore energy flux =
$$\sum_{n=1}^{N/2} \gamma 2 [a(n)^2 + b(n)^2] C_g(n) \cos \Theta(n)$$

= $\frac{\gamma E_b^2}{8} C_{gb} \cos \Theta_b$ (22)

Assuming that the breaking wave angle, Θ_b , is small, that the waves will break under shallow-water conditions, and that the ratio of breaking wave height to depth is a constant, the breaking wave height, H_b , is then given by

$$H_{b} = \left\{ \sum_{n=1}^{N/2} 16 \left[a(n)^{2} + b(n)^{2} \right] C_{g}(n) \cos \Theta(n) \right\}^{0.4} \left(\frac{GB}{g} \right)^{0.2}$$
(23)

where GB is the ratio of root-mean-square (rms) breaking wave height to breaking depth, GB = H_b/d_b (here assumed GB = 0.78). With the breaking depth known, each wave component is transformed to shore accounting for both wave refraction and shoaling based on linear wave theory.

Wave refraction is in accordance with Snell's law and the assumption that straight and parallel contours existed between the gage and breaking locations

$$\Theta_{b}(n) = \sin^{-1} \left[\frac{C_{b}}{C_{r}(n)} \right] \sin \Theta_{r}(n)$$
(24)

where C is linear wave celerity (see the SPM, Ch. 2) in which the r subscripts denote the "reference (gage)" location.

With the wave energy and direction now known at the breaker line, the value of the longshore energy flux, $(P_{1s})_{cm}$, is readily determined

$$(P_{ls})_{cm} = R(P_{ls})_{c}$$

$$= R \left\{ 2\gamma \sum_{n=1}^{N/2} [a^{2}(n) + b^{2}(n)]_{b} [C_{g}(n)]_{b} [\cos \Theta(n) \sin \Theta(n)]_{b} \right\}$$
(25)

in which the factor R is given by the ratio

$$R = \frac{E_{TOT}}{E}$$

as defined in and discussed in relation to equation (21).

III. MAIN PROGRAM DOCUMENTATION

The detailed programing steps in analysis for the longshore energy flux, $(P_{\ell,S})_{\rm Cm}$, (which in this program is calculated in terms of rms wave height) are presented in this section. Program steps are numbered to correspond to areas in the program listing where computations are carried out. A program listing with corresponding numbered steps follows the program documentation. Note that preceding text has used the indexes j and n for time and frequency, respectively, while the program which follows uses the index I for both time and frequency. A listing of the main program is presented in Figure 2. Program steps are as follows and refer to numbered parts of main program listing:

1	c c	PROGRAM SPECT(INPUT,OUTPUT,TAPES=INPUT,TAPES=OUTPUT,TAPES) Cumputor algorithm to calculate longsmore energy flux factor and wave Direction for two pressure sensor arkay
5	ĉ	MAIN PRUGRAM PRUGRAM IS PRESENTLY SET UP TU TAKE A TIME SERIES OF 1024 POINTS IN MAIN DIMENSION ((512)
		DIMENSION FIR(1024)+FII(1024)+F2R(1024)+F21(1024) UIMENSION SIGMA(512)+FMODSQ(518)+THEIA(512) DIMENSION CI2(512)+012(512)
10		DIMENSION W(1024) DIMENSION CG(512)+BINTHB(512) REAL MEANI,MEAN2 LOGICAL END
15	c 101	DATA END/,FALBE./ FUHMAT(10(2X+FS,2))
		DEFINITIONS-FIXED VAMIABLES Kalkpunential pomer defining numger uf time behies pointa=(2**k)
50		S#SPACING BETWEEN WAVE GADES (PEET) Delit#Time BTEP BETWEEN POINTS IN AVERAGED TIME BERIES (SECONDS) BETA #ANGLE DIFFRENCE BETMEEN WAVE GAGE ALIGMMENT AND SHORELINE(RADIANS SLOPE#SLOPE OF BEACH AT PUINT OF WAVE BREAKING
25	ç	GAMMA#SPECIFIC WEIGHT OF FLUIO (L85/F1#43) B#DIBTANCE OF PRESSURE SENSORS ABOVE BOTTOM (FEET) G#ACCELEKATION OF GRAVITY (FEET/SEC##2)
	с . с	GB#RATIO BREAKING WAVE HEIGHT/DEPTH FOR LINEAR THEORY COMPUTATION OF wave height GB#Paratu breaking wave height/depth for linear theory computation of
30	Ċ C C	WAİER DEPTH GIVEN BREAKING MÄVE HEIGHT
35	ĊĊĊ	DEFINITIONS=FLDATING VARIABLES Avgi=Average of time Seriesi Avg2=Average of time Series 2
	с с с	C(1)=WAVE CELERITY Cla(1)=COSPECTRA OF SERIE01=2 CB#BREAKING WAVE CELERITY
40		LG(1)=URUUP WAVE CELENITY CNTL(1)=URUOPA DOINT TIME SENIES BEFORE AVERAGING DEPTH=DEPTH UF WATEN AT GAGE SITE FRUM AVERAGES UF GAGES 1 AND 2 F11(1)=UNDEFINED/COMPLEX INAGINARY PUNTION OF TRANSFORM F11(1)=TIME SERIES DATA GAGE1/COMPLEX REAL PURTION OF TRANSFORM
45	0 0 0 0	F2I(I)#UNDEFINED/COMPLEX IMAGINARY PURTIUN OF TRANSFORM F2M(I)#TIME BERIES DATA GAGE2/COMPLEX REAL PURTION OF TRANSFURM FMDDSq(I)#TIME SERIES AMPLITUDE MODULUS SQUARED HB#RHEAKING MAYE MEIGHT
\$0		IACIJESOOO POINT DATA GRUUP AND TIME BENIES RECURD PLNEGENEGATIVE CUNTRIRUTIUN TU LUNGSMUHE ENERGY FLUX FACTOR PLNETENET LUNGSNURE EVERGY FLUX FACTOR PLPOBEDGITIVE CUNTRIKUTIUN TU LUNGSMUHE ENERGY FLUX FACTOR
55		WIZ(I)=UUADSPECTRA OF SERIES I=2 H=SCALING FACTOR FOR SCALING UP ENERGY OF NONUSABLE Purtions of directional specific formations of the series of the same second s
	C C C	RATIUZENATU OF ENERGY/WINDUWED ENERGY FUR GAGE 2 REAL(I)#1024 POINT TIME SERIES AFTER AVENALING HN#RATIO OF GROUP WAVE CELERITY TO WAVE CELERITY
60	0 0 0 0	MSHRAUBPERCENT OF ENERGY BEYUNU SPACIAL ALIASING FREUUENCY HSLFRG≣PERCENT OF ENERGY BELUN LOW FREUUENCY CUTUFF HSUDU≣FERCENT UF INCUMENENT ENENGY SMFREUBBUM UF ENERGY MITH FREUÜENCIES ABOVE SPACIAL Aliasing Eveniegy cutofe
65	с с с	SIG2#SUMMATION OF ONSHORE ENERGY FLUX SIGMA(1)#FRADIAL FREQUENCY SLFREQ#SUM OF ENERGY WITH FREQUENCIES BELOW LOW FREQUENCY CUTOFF SUDDESUM OF FNERGY WITH FREQUENCIES BAUING INCOMEDENT WAVE OTDECTION
70	000	SUMENISUM OF SQUARES OF TIME SEMIES 1 WITHOUT AVERAGE SUMISSUM OF SQUARES OF TIME SEMIES 1 WITHOUT AVERAGE
		SUMF2#SUM OF SUDAMES OF TIME SERIES 1 WITH AVENAGE SUMF2#SUM OF SUDARES OF TIME SERIES 2 WITH AVENAGE Tewave Period Theta(1)#Wave direction in Hadians

Figure 2. Listing of main program.

75	C C C	THETABBBHEAKING WAYE ANGLE WSUM1#SUM OF SQUARES OF DATA WINDDW HODIFIED TIME SERIES 1 WSUM2#SUM OF SQUARES OF DATA WINDDW HUDIFIED TIME SERIES 2 P1#3,14159265 THUP1#2.0491
80		N=10 N=2.**K S=00 DELTI=1.00 BETA=1.5708
35		SLOPE=0,05 GAMMA=60,0 B=2.5 M=N=1 ND2=N/2
9 0		GB#0,78 G=32.2 GRP=0.78
	ç	HIGH FRED CUTOFERT.O SEC
95	č	SPACIAL ALIASING CUTOFF#3.4 SEC
	Ć	NLOWALOW FREQUENCY CUTOFF NUMBER
	ç	NYFREMIGH FREQUENCY CUTOFF NUMBER
	ç	NSALFRESPACIAL ALIABING FREQUENCE CULUPP NUMBER
100	č	ANERGENET COLOFY NONDERSTAND CONSERVED FENDING COLOFY CONSERVED
	•	NLOw=50
		NYFR=342
		NSALFK#301 NSM1#NSA1FD_1
105	110	CUNTINUE
	ç	INITIAL TETNE VALUES
		SUDO=0.0
110		SMFREGEO.0
		8UM1=0.
		SUM2=0.
		SUMF1=0.
		SUMF 2mg.
113		wSUM1=0.0
		WSUM2=0.0
		VAC300"0
120		PLP08=0.0
		PLNEG=0.0
		FLNE1#0.0
		00 29 I=1.N
125		F11(1)=0,0
		F21(1)=0.0
	29	CUNTINUE
		FMUDSQ(1)=0.0
130	30	CONTINUE
	ç	THE DEPART OF DECEME DEADS IN MAVE PRESSURE VALUES INTO FIRAFER ARRAYS
	C	AND ASSURES MATCHING DATE GROUPS FOR DIRECTIONAL WAVE ANALYSIS OF TWO
	č	GAGES, TATAL THE THE THE THE THE
135		CALL BUF(MGAGE1.MONTH1.MOAY1.MTIME1.FIN
		CALL RUF (MGAGE2. MUNTH2. HDAY B. MIIME2. F2H . IDATE2. END)
		IF(ENU) GD TO 1
		IF(IUATE1.E0.IDATE2) GD TU 120
		Complement

Figure 2. Listing of main program.--Continued

140	BACKSPACE 9 GU TU 110 120 CONTINUE
145	ARTHORNELLARESIL) CALL BAILTHARAGELARGAGEZARIK APER) WRITE(6+426) 426 FURMAT(///I GAUGE NU. (+6X+(MUNTH(+TX+(CAY(+8X+(TIME() WRITE(6+1))MGAGEL+MONTH(+MAX)+MTIMEL
	WHITE(6,11)MGAGE2,MONTH2,MDAY2,MTIME2 11 FUHMAT(17,3(5%,17))
150	THIS PORTION OF PROGRAM CALCULATES WATER DEPIH AT WAVE GAGES AS WELL AS AVEHAGES AND SUM OF SQUARES OF TIME BERIES OD 43 Taily
155	A UGI mavGI+FIR(1) 42 A VG2mavG2+F2R(1) A VG1mavG1/FLOAT(N) A VG2mavG2/FLOAT(N)
160	DEPTH=(AVG1+AVG2)/2.+8 CALL HFC(DEPTH;8:0ELTT;N:N8ALFM) OU 41 Imi;N F1H(1)=F1R(1)=AVG1
	8UM1=8UM1+F1R(J)**2. 8UM2=8UM2+F2R(J)**2. 41 LONTINUE
165	SUM1#SUM2/FLUAT(N) SUM2#SUM2/FLUAT(N)
170	THIS PORTION OF PHUGHAM APPLIES DATA WINDOW TO TIME SERIESDATA WINDOW VALUES ARF REPRESENTED BY W(Ì) DU B9 Imi,N W(I)=0.5*(1.0-CHS(TWUPI*FLUAT(I)/FLUAT(N)))
	FIR(I)=(FIR(I))*W(I) F2R(I)=(F2R(I))*W(I) A9 CUNTINUE
175	THIS PORTION OF PROGRAM COMPUTES SUM OF SQUARES OF DATA WINDOW MODIFIED Time Beries as well as ratio of pre windowed energy to windowed energy OU 43 Iml.N
180	<pre>%5UM1=#sUM1+F1R(1)**2。 #5UM2=#sUM2+F2R(1)**2。 43 CUNTINUE #5UM1=#sUM1/FLOAT(N) #5UM2=#sUM2/FLOAT(N)</pre>
185	HAIIU]#SUMI/WSUMI HAIIU2#SUM2/WSUM2 CALL FFT(F]R*FII*K*0) CALL FFT(F2R*F2I*K*0) MEAN2#F2R(1)
140	THIS PURTION OF PROGRAM CALCULATES CO AND QUAD SPECTRA VALUES, AS WELL AS Mave angle to shoreline and energy contributions of each frequency, bheaking mave height and bheaking wave celerity are also calculated by this section.
195	1=1 00 97 J=2,N FIR(1)=F1R(J) FII(1)=F1I(J)
005	+2M(1)=F2R(J) F21(1)=F2I(J) I=I+1 97 CONTINUE 00 9 I=I+M
	SUMF1=SUMF1+F1R(1)**2.+F11(1)**2. Figure 2. Listing of main programContinued

205		SUMF2=SUMF2+F2R(I)++2,+F2I(I)++2,
	90	CUNTINUE
		SUMFIESUMFIEMFANIES.
		SUPPERSUPPERMENTE.
		WRITE(6+2A9]
210	289	FURMAT(//+7x+(I(+10x+(SIGMA(1)(+11x+(FMDBQ(I)))
		00 99 T=1-NO2
		els(r)s.lk(l)+.Sk(l)+.lt(r)+.st(l)
		Q12(1)=F1R(1)+F2I(1)=F2R(1)+F1I(1)
		SIGMA(I)=FIUAT(I)+TWUPT/(FLDAT(N)+DFLTT)
215		
512		1-1H0F1/016HA(1)
		GALL WVLEN(DEPTH.T.XKH)
		XK=XKH/DEPTH
		IF(C12(1)) F-0.000000011 G0 TU 98
		POP/1 //YEARING ATAN/DISC/TI//CIS/TIS
220		IF(AB8(PD).GT.1.0) GU 10 43
		THETA(I)==ACOS(PD)+BETA
		60 TU 92
		THETACTOR
	*3	IncleCIJ=0+0
		GU TU 92
225	93	THETA(1)=0.00001
	-	AMUDSOLTIACIBLIARS ACTIVIARS
		The second state in the second state second se
		XVB3XKH48/DFh1H
		XKP=CUSH(XKB)/CDSH(XKH)
		FMUDSU(I)#FMDDSD(I)/(XKP##2.)
270		
230		rivb3d(1)=Pilb5b(1)+Raf101
		SUDD#SUDD+FMUDSG(I)
		WRITE(0.105)I.SIGMA(I).FMUDSU(I)
	105	FURMAT(31.15.51.F12.6.71.F18.6)
	105	
	46	CONTINUE
235		FMUD80(I)#F1k(I)++2++F1I(I)++2+
		XKBRAKHABZOEPTH
		XKPaCUBuCXXB3 (COBHCXXH3
		PHUDSG(1)=PHDDSG(1)/(AKP+72.)
		FMUDSQ(I)=FMUDSQ(I)=RATID1
240		RN#0.5+(1.+2.+XKH/8INH(2.+XKH))
-		CG(T) ROTCHAFT) ODERTHARN /YKH
		CALL BIR WALL FUR FILL WALKAN
		C(I)=CG(I)/RN
		MG2=(CG(I)+2,0+FMUDSU(I)+CO8(THETA(I)))
c c		SHG2=ONSHDRE FNERGY FLUX
245		SHG288HG34HG2
247		
		SOUGUESOPENAPPHODSO(1)
		IF(I.GE,NSALFR) GO TU 79
		GO TO YA
		SHEPED-BURDENARMODOC/TY
	- 17	Shir heusen reuser house (1)
250	78	CONTINUE
		IF(I.LE.NLOW) GO TO 77
		GO TO 76
	- 11	arrea-orreasenousa(1)
	76	CONTINUE
255		1F(1.GE.NYFR) GD TO 999
	0.0	CONTINUE
	444	CONTINUE
		5HG2#5HG2#2.
		WRITE(6+351)
34.0	751	FORMAT/ / / V. / T / . SHY . INTOMATTS F POT /
200	321	
		nn de Televins
		IF(I.GE.NBALFR) GD TO 44
		PCT=FMODSQ(1)/SUMEN
		IF(PCT GE & ADE) GO TO #9
203		00 10 48
	49	WRITE(6+50)I+BIGHA(I)+PCT+THETA(I)
	50	FURMAT(3x+15+3(3x+F16+8))
	48	CUNTINUE
	40	
	44	CONTINUE

Figure 2. Listing of main program .-- Continued

270	57	HB#(B.***'4)*(8H65**'4)*(8A'C)**'5 CP#(0*HB/0HP)**'2 CNulive
	ç	THIS PURTION OF PROGRAM MUDIFIES HAVE GAGE ANGLES TO BREAKING HAVE ANGLES
277	τ	AND CUMPUTES LONGSHORE ENERGY FLUX FACTONS DU 91 Im1.ND2 IF(1.GE.NSALFR) GO TO 998 SINTHF(1.BESINTHFTA(1))*CB/C(1)
280		THETAH=ABIN(SINTHB(I)) XKHS=((1.+SIN(THETA(I))**2.)/(1.=SINTHB(I)**2.))**.5 XKSSmCG(I)/CB FMUSSU(1)#FMUSSG(I)*XKRS*XKSS
3.05		IF(THETA(1),LE,0,0) 60 TU 87 PLP03#PLP03+PLP03+GAMMA*SIN(2,*THETA8)*C8+FM00SQ(1)
405	87 85	GU TU BA PLNEGEPLNEG+GAMMA*SIN(2.*THETAB)*C8*FHUD5Q(1) CUNTINUE
290	91 998	PLWEISHNET+PL PLWEISHNET+PL IF(I.GE,NYFR) GO TO 998 CONTINUE CUNTINUE
295		HSUDU=SODJSUHEN HSHFRU=SHFREJ/SUHEN HSLFHU=SLFREJ/SUHEN HTUT#RSUD+HSHFRQ HTI_T#RSUD+HSHFRQ
300		PLPU8#PLPU\$4R Plnetaplneg4r Plnetaplnet4r Write(6,201)nsalfr
105	500	FURMAI(//*(NSALFHE(*24X*46) WRITL(6*200)DEPTH FURMAI(1 DEPTH OF WATER AT GAUGE SITE=(*F10,1) WRITE/6*1001augi-aug2
	100 170	FUMMAT((AVG1=[+F11,]+9X+(AVG2=[+F11.3) #RITE(6+170)30M1+80H2 FUMMAT(1 80M1=(FF11.3+9X+(80M2#[+F11.3)
310	111	m=ITE(6+111)#8Un1+*SUM2 Fukmat((#8Um1m=(*F10+3;9X*(#8UM2m=(*F10+3) ##ITE(6+112]#at1U1=Rat102
	39	FUMMAT((MATIOIm (+F9.3,9X+ (MATIO2m (+F9.3) MATTE(6.35)SUMEN FUMMAT((SUMENA (+2X+F13.5)
315	104	MYIIE(6+104)HB Format((Bheaking wave height mb=[+6x+f10,2) MyIte(6+108)CB
320	108	FURMAT(1 BREAKING WAVE CELENITY CBmt,4%,F10,2) white(6,106) rsodd,rsmfro,rstfng Format(1 Rsuddmt,rf11,4,8% (KShfromt,F10,4,8%, (KSLFROm(,F10,4)
	103	WRITE(6+103)PLPOS+PLNEG FURMAT([PLPUS=(+f11.4+8x+(PLNEG#[+f11.4) WRITE(-103)PLNE(-f11.4+8x+(PLNEG#[+f11.4))
375	109	FORWAT((PLNET=1+F11+4) GU TU 110 CUNTINUE STOP ENU

Figure 2. Listing of main program.--Continued

(1) Input data for this program are in the form of digital magnetic-tape records of 4,100 values. The first 4 values of the records are the gage number, month, day, and time of the observations; the last 4,096 values are the time-series pressure values of the wave gage. In the present program the wave gage pressures are stored in thousandths of a foot (head) water at 0.25-second intervals. Subroutine BUF reads time-series data into array CNTL, where it is averaged to provide 1,024 time-series values of $\Delta t = 1$ second spacing. Units are also divided by 1,000 to convert values to feet (head) of water.

(2) The date groups of record 1 and record 2 are compared to ensure that times of records are simultaneous; if the times are not, the program searches the record file until this condition is met. The two records are than checked for proper sequence to ensure that gage 1 is analyzed first. Subroutine SWITCH switches arrays if they are not in proper order.

(3) Each of the two 1,024 value time series is then analyzed for average values which are printed out along with the average depth of water at each gage site. The average value of each of the timeseries records is again averaged and is added to the height of the gages above the bottom to obtain the water depth:

$$DEPTH = \frac{AVERAGE 1 + AVERAGE 2}{2} + B$$

in which AVERAGE 1 is the average of time series $1 = a_1(0)$, AVERAGE 2 the average of time series $2 = a_2(0)$, and B the height of sensors above the bottom.

An option to apply a weighting function w(j) (= W(I) in program) has been incorporated before the FFT subroutine is called. In this particular program a cosine bell weighting function has been incorporated. If the data window option is selected, the two time-series data records, which are read into F1R and F2R arrays, are multiplied by the following weighting function (cosine bell)

$$w(j) = \frac{1}{2} \left[1 - \cos\left(\frac{2\pi j}{N}\right) \right]$$

where j is the time step number and N the number of data points in series. If no weighting function is desired in analysis set w(j) = 1.0, which is the "box car" weighting function.

As the cosine bell function reduces the total energy content of the waves, the final energy obtained from the FFT must be rescaled up to the proper value. This is accomplished by scaling up the timeseries pressure values by the ratio

$$R = \frac{\text{Unwindowed energy}}{\text{Windowed energy}} = \sqrt{\frac{\langle p^2 \rangle}{\langle p^{+2} \rangle}}$$

as discussed in equation (4).

(4) Cospectra and quad-spectra of the gages are computed using the following relationships (note in computer program index, I is used for frequency counter, n):

$$Cospectra = C12(I) = F1R(I)*F2R(I) + F1I(I)*F2I(I)$$

$$Quad-spectra = Q12(I) = F1R(I)*F2I(I) - F2R(I)*F1I(I)$$

in which F1R and F1I are the real and imaginary parts of complex transforms of time series 1: F2R and F2I are the real and imaginary parts of complex transforms of time series 2.

(5) Wave angle is calculated in accordance with equation (19).

$$\Theta(n) = \Theta = \frac{\beta}{\arccos ne} \left[\frac{1}{k(n)\ell} \cdot \arctan \frac{Q12(n)}{C12(n)} \right]$$

where k(n) is the wave number calculated via linear wave theory, ℓ the spacing of gages, and β the difference in alinement of gages and shoreline in Figure 1.

Due to energy leakage problems in spectra, impossible wave angles can result [wave angles with $(1/k(n)\ell \arctan Ql2(n)/Cl2(n))$ greater than 1.0]. When this happens, energy is lumped into a separate category for later scaling up of the longshore energy flux.

(6) The high frequency cutoff in this particular program has been set at 2.09 radians per second, which corresponds to a period of 3 seconds or NYFR = 342. This value can be reset in the main program by adjustment of NYFR where

$$VYFR = \frac{N\Delta t}{T_{HF}}$$

and N is the number of data points in time series, Δt the spacing in time of data points, and $T_{\rm HF}$ the high frequency cutoff period. The spatial aliasing frequency is computed in subroutine HFC.

Energy between the spatial aliasing frequency and the high frequency cutoff is put into a special category and used to scale up the final longshore energy flux.

(7) Each frequency contribution to the onshore energy flux is calculated for the gage site location as follows:

Onshore energy flux =
$$2\gamma |F_{\eta}(n)|^2 C_g(n) \cos [\Theta(n)]$$

where

F _η (n)	=	modulus of the complex amplitude spectra of wave elevation above mean surface at gage site
C _g (n)	= .	group wave speed at gage site
Θ(n)	=	0 = angle of wave direction (see Fig. 1)
γ	=	specific weight of seawater

The onshore energy flux is then summed to obtain the total onshore energy flux. In the program, onshore energy flux/ γ = HG2.

(8) Breaking wave height at the shoreline is determined from the mean square onshore energy flux via a linear theory wave transformation formula which can be simplified to

$$H_{b} = \left[\sum_{n=1}^{N/2} 16 |F_{n}(n)|^{2} C_{g}(n) \cos \Theta(n)\right]^{0.4} \left(\frac{GB}{g}\right)^{0.2}$$

where GB is the wave height-to-water depth ratio at breaking and g the acceleration of gravity.

The choice of GB is up to the user although a value of GB = 1.42 has been found by Komar and Gaughan (1972) to best fit wave tank data for breaking wave heights for monochromatic waves. In the present program, GB has been set equal to 0.78 but can be readily changed.

The breaking wave water depth is calculated from the equation

$$\frac{H_{b}}{d_{b}} = GBP$$

where d_b is the wave breaking water depth and GBP the ratio of wave height to water depth at breaking.

In this case a different value of the ratio of breaking wave height to water depth can be used in the program for obtaining the proper water depth. An assumed value of GBP = 0.78 from the solitary wave theory in the SPM is used.

Linear wave celerity is assumed and breaking wave celerity is estimated as

$$C_{\rm b} = \left({\rm g} \frac{{\rm H}_{\rm b}}{{\rm GBP}} \right)^{0.5}$$

The breaking wave height and celerity calculated in this approach apply to all frequencies.

(9) Frequency-by-frequency modification of wave angles is made assuming linear wave theory, Snell's law, and parallel bottom contours offshore. The breaking wave angle, $\Theta_{\rm b}(n)$, is calculated from

$$\Theta_{b}(n) = \arcsin\left[\frac{C_{b}(n) \sin \Theta_{r}(n)}{C_{r}}\right]$$

where the subscript r refers to the reference gage location.

(10) Longshore energy flux is calculated for each frequency component (except the special cases discussed in Sec. II) using the equation

$$P_{ls}(n) = \gamma |F_n(n)|^2 C_{gb}(n) \sin 2\Theta_b(n)$$

and is summed up to obtain a net longshore energy flux.

(11) The value of the net longshore energy flux is multiplied by a factor R which scales up the total energy in the spectrum (below the high frequency cutoff). The equation for scaling factor R is

$$R = \frac{1}{(1 - RTOT)}$$

where RTOT = RSODD + RSHFRQ when RSODD is the percent of energy in low frequency bands for which impossible values of the cosine function are calculated, and RSHFRQ is the percent of energy between spacial aliasing frequency and high frequency cutoff.

The final result of analysis of the two gage records for the net longshore energy flux PLNET is printed out, as well as specific frequencies for which impossible directional results occur and frequencies at which more than 2.5 percent of the total wave energy is found.

IV. SUBROUTINE DOCUMENTATION

1. FFT Subroutine.

The sampled time function, f(j), will be expressed as

$$f(j) = \sum_{n=0}^{N-1} F(n) \exp(in\omega_1 j \Delta t)$$

in which

$$\omega_{1} = \frac{2\pi}{\text{record length}} = \frac{2\pi}{T} = \frac{2\pi}{N\Delta t}$$

$$t_{j} = j\Delta t = a \text{ discrete time where } j \text{ is the integer time step}$$

$$F(n) = a(n) - ib(n)$$

$$a\left(\frac{N}{2+n}\right) = a\left(\frac{N}{2-n}\right) , n \neq 0 , \frac{N}{2}$$

$$b\left(\frac{N}{2+n}\right) = -b\left(\frac{N}{2-n}\right) , n \neq 0 , \frac{N}{2}$$

$$a(0) = \text{mean of sampled record}$$

$$b(0) = b\left(\frac{N}{2}\right) = 0$$

Because negative indexes are not readily handled by most FORTRAN compilers, the summation extends over the interval $0 \le n \le N - 1$, rather than over the symmetric interval $-N/2 \le n \le N/2$. From the definition of the coefficients above, it is clear that the coefficients a(n) and b(n) for n > N/2 contain no additional information.

The inverse relationship completing the FFT pair is

$$F(n) = \frac{1}{N} \sum_{j=1}^{N} f(j) \exp(-in\omega_{j} \Delta t)$$

As an enumeration of the complex FFT coefficients, suppose the series of 8 values is considered, N = 8. The coefficients would be

$$F(0) = a(0)$$

$$F(1) = a(1) - ib(1), F(7) = a(7) - ib(7) = a(1) + ib(1)$$

$$F(2) = a(2) - ib(2), F(6) = a(6) - ib(6) = a(2) + ib(2)$$

$$F(3) = a(3) = ib(3), F(5) = a(5) - ib(5) = a(3) + ib(3)$$

$$F(4) = a(4)$$

This pattern prevails for all sets of FFT coefficients, regardless of the value of N. Both F(0) and F(N/2) are real and, as noted previously, the coefficients F(n) for n > N/2 really contain no additional information. The FFT subroutine used here requires that the number of data points, N, provided be an integral power of 2, i.e.,

$$N = 2^{K}$$

where K is an integer. Thus analyses of 512, 1,024, or 2,048 data points (K = 9, 10, 11) would be suitable with this subroutine.

The following two requirements are satisfied in the FFT subroutine.

(a) By operating on the sampled function, obtaining the F(n) coefficients and carrying out the inverse FFT (FFT⁻¹), the original time function is recovered. Schematically,

$$f(j) + FFT + F(n) + FFT^{-1} + f(j)$$

(b) The mean square of the sampled time function is equal to the sum of the squares of the moduli of the FFT coefficients, F(n), i.e.,

$$\frac{1}{N} \sum_{j=1}^{N} [f(j)]^2 = \sum_{n=0}^{N-1} |F(n)|^2$$

a. <u>Calling Statement</u>: SUBROUTINE FFT (FR, FI, K, ICO) (see Fig. 3). FR, FI = real and imaginary coefficients in

$$F(n) = FR(n) - iFI(n)$$

 $K = power of two (i.e., N = 2^K)$

 $ICO = control whether FFT or (FFT)^{-1}$

operation is desired if

$$ICO \begin{cases} = 0 \neq FFT \\ = 1 \neq (FFT)^{-1} \end{cases}$$

When entering the subroutine, FR is the time sequence f(j) and FI is arbitrary. When exiting the subroutine, FR and FI are the real and imaginary parts of the complex transform, respectively; e.g., input is

$$K = 5$$

ICO = 0
$$f(j) = 1.0 + 2.0 \cos \frac{2\pi(j\Delta t)}{32} + 3.0 \cos \frac{4\pi(j\Delta t)}{32}$$
$$- 0.6 \sin \frac{2\pi(j\Delta t)}{32} - 1.4 \sin \frac{4\pi(j\Delta t)}{32}$$

1	c	
	C	FAST FOURIER THANSFORM SUBROUTINE
		SUBRUUTINE FFT(FH+FI+K+ICO)
		UIMENSION FR(1)+FI(1)
5		N22++K
		IF(ICO.EG.O) GO TO IO
		FILIJ##FILIJ
1.0	10	MWB0
10		NNENet
		DU 2 Matenn
		LEN
	1	L=L/2
15		IF(MR+L.GT.NN) GU TO 1
		MR=MUD(MR+L)+L
		IF(MH.LE.M) GO TO 2
		TR=FK(M+1)
		FR(M+1)#FR(MR+1)
50		FH(MR+1)=TR
		TI#FI(M+1)
		FI(M+1)=FI(MR+1)
		Plime+1)stI
	ć	LONTINUE
25		
	3	IF(LeGE_N) GO IO /
		TOILLESSE
		DO 4 Metal
10		ART. 1418004 STRAFI DAT(1-M)/FI
30		WHECOBIAN
		WISSIN(A)
		DO 4 INMANAISTEP
		J=I+L
35		IF(ICU.E0.1) GO TO 11
		TREWR*FR(J)=WI*FI(J)
		TI#WH*FI(J)+WI*FR(J)
		GO TU 12
	11	TR#WR#FR(J)+WI#FI(J)
40		TI#WR*FI(J)=WI*#R(J)
	12	FR(J)=FR(I)=TR
		F1(J)#F1(I)=FI
		E2(1)===(1)+1H
45	۳	FICI)=FICI)+II
43		
	7	CONTINUE
		ANEN
		IF(ICO.EQ.1) 00 TO 6
50		00 5 I=1.N
•••		FR(1)=FR(1)/AN
	5	F1(1)==F1(1)/AN
	6	RETURN
		ENU

Figure 3. Listing of FFT subroutine.

b. Data Input to Program.

f(j) values at	6.000	5.080	3.750	2.184
$\Delta t = 1$ second	0.590	-0.829	-1.900	-2.506
intervals	-2.600	-2.215	-1.451	-0.465
(32 values)	0.562	1.445	2.034	2.229
	2.000	1.391	0.513	-0.475
	-1.390	-2.054	-2.322	-2.109
	-1.400	-0.257	1.188	2.755
	4.238	5.438	6.189	6.386
FR =	6.000	5.080	3.750	2.184
(32 values)	0.590	-0.829	-1.900	-2.506
	-2.600	-2.215	-1.451	-0.465

		0.562	1.445	2.034	2.229
		2.000	1.391	0.513	-0.475
		-1.390	-2.054	-2.322	-2.109
		-1.400	-0.257	1.188	2.755
		4.238	5.438	6.189	6.386
	FI =	0.000	0.000	0.000	0.000
	(32 values)	0.000	0.000	0.000	0.000
		0.000	0.000	0.000	0.000
		0.000	0.000	0.000	0.000
		0.000	0.000	0.000	0.000
		0.000	0.000	0.000	0.000
		0.000	0.000	0.000	0.000
		0.000	0.000	0.000	0.000
c.	Calling Statement:	FFT (XR,	XI, 5, 0).		
	Output:	1.000	1.000	1.500	0.000
	a(n) coefficients	0.000	0.000	0.000	-0.000
	(32 values)	-0.000	-0.000	-0.000	-0.000
		-0.000	-0.000	-0.000	-0.000
		-0.000	-0.000	-0.000	-0.000
		-0.000	-0.000	-0.000	-0.000
		-0.000	0.000	0.000	0.000
		0.000	0.000	1.500	1.000
	b(n) coefficients	0.000	-0.300	-0.700	-0.000
	(32 values)	-0.000	-0.000	-0.000	-0.000
		-0.000	-0.000	-0.000	-0.000
		-0.000	-0.000	-0.000	0.000
		0.000	0.000	0.000	0.000
		0.000	0.000	0.000	0.000
		0.000	0.000	0.000	0.000
		0.000	0.000	0.700	0.300

 Δt (time step) = 1 second in above example.

2. HFC Subroutine.

This subroutine resets the spatial aliasing frequency cutoff to a higher frequency than would be the case for normal incidence of waves to gage pair. In the present version of this subroutine, it has been assumed that the maximum angle which the wave crests can make with the gage pair axis is 45°. The spatial aliasing criteria are expressed in Figure 1, where for proper resolution of wave direction the following criteria must be met

$$l\cos \left[\Theta(n) - \beta\right] < \frac{L}{2}$$
$$k(n) l\cos \left[\Theta(n) - \beta\right] < k(n) \frac{L}{2}$$

The proper spatial aliasing frequency to correspond with the spacial aliasing wave number cutoff is found from the normal wave dispersion relationship.

Calling Statement: HFC (DEPTH, S, DELTT, N, NSALFR) (see Fig. 4). DEPTH = depth of water at gage site (from main program) S = spacing of wave gage pair (from main program) (= & in text) = time-step increment between values in time series analyzed DELTT (from main program) N = exponent of 2 describing number of time series values (from main program) NSALFR = integer number for spatial aliasing frequency cutoff 1 ç SUBRUUTINE HECCHIGH FREQUENCY CUTOFF/SPACIAL ALIASING FREQUENCY) HESETS ALIASING CUTUFF TO HIGHER FREQUENCY HASED UN ASSUMED MAXINUH WAVE ANGLE SUBRUUTINE HFC(DEPTH+8+DELTT+N+N8ALFR) C C 5 SPACIAL ALIASING ASSUMES WAVE ANGLES LESS THAN 45 DEGREES с XK8=3,14159/0,707 XKH=XK6+DEPTH/S SIGSU=32.2+(XKH/OEPTH)+TANH(XKH) SIGHF=BORT(SIGSO) HECLN=FLOAT(N)+DELTT 10 NSALFH#SIGHF*RECLN/6.283 RETURN END

Figure 4. Listing of HFC subroutine.

3. SWITCH Subroutine.

1

This subroutine is set up to interchange time-series data arrays in the instance when gage 2 data are processed before gage 1 data (see Fig. 5). If the first gage record processed is not equal to the appropriate number of the gage, as specified in main program, data arrays of first and second gage records are interchanged.

C C SUBRUUTINE SWITCH EXCHANGES LUCATIONS OF TIME SERIES DATA TO ASSURE GAGE1 18 STORED IN FIRST ANRAY AND GAGE2 IN SECOND SUBRUUTINE SWITCH(M1.M2.FIR.F2R) C DIMENSION FIR(1024) . F2R(1024) . F3R(1024) 5 MBEMI MISHR H2=H3 DO 10 1=1+1024 10 F3R(I)=F1R(I) FIR(I)#F2H(I) F2H(I)=F3R(I) 10 CUNTINUE RETURN 15 ENĎ

Figure 5. Listing of SWITCH subroutine.

4. WVLEN Subroutine.

This subroutine accepts wave period and water depth as input and calculates wave number as output via a Newton-Raphson iteration.

Calling Statement: WVLEN (DPT, PER, XKH) (see Fig. 6). DPT = water depth (from main program) PER = wave period (from main program) XKH = wave number * water depth (calculated in subroutine) 1 C C WAVE LENGTH ITERATION SUBROUTINE ... THIS SUBROUTINE CALCULATES WAVELENGTH VIA NEWTON-RAPHBON ITERATION USING PERIOD, WATER DEPTH INPUT CCCC PERSWAVE PERIOD OPTSWATER DEPTH 5 XKHEWAVE NUMBERSWATER DEPTH SUBROUTINE WYLEN(DPT, PER, XKH) 1KH0= (6.2831853/PER) ++2+0PT/32.2 IF (XKH0=6.3)2.1.1 10 1 XKHEXKHD GO TO 9 2 XKH#SURT(XKHU) 3 SHESINH(XKH) CH#CUSH(XKH) 15 EPaskHU-XKH+8H/CH SLUPE==XKH/CH##2=8H/CH DXKHE-LPB/SLOPE IF (AB8(DXKH/XKH)=0.0001)9+9.4 4 XKH#XKH+DXKH GU TU 3 9 CUNTINUE RETURN **FNÓ**

Figure 6. Listing of WVLEN subroutine.

5. BUF Subroutine.

This subroutine is set up to read in wave gage files from magnetic tape. The data records consist of arrays of 4,100 values, the first four of which are the gage number, month, day, and time of wave record. The remaining 4,096 values represent pressures in thousandths of a foot (head) water. The data are returned to main program as a wave gage number-date series and a time series of 4,096 values of pressure in feet (head) of water. Two records are processed in one pass.

Calling Statement: BUF (MGAGE, MONTH, MDAY, MTIME, CNTL, IDATE, END) (see Fig. 7).

MGAGE = number of gage (read from tape)

MONTH = month of observation (read from tape)

MDAY = day

MTIME = time

CNTL = control array of 4,096 pressure values in feet (head) of water returned to main program

IDATE = summed time group for time comparison between gages

END = logical end

	r	
	č	SUBPOSITING MUR DEADS IN WAVE GACE DATE INFO AND TIME SERIES DANAMIC
	ž	Descripte but we the first what the bate
	Ļ	THESSURE VALUES IN FEEL HEAV OF WALER VALUES AND AVEDACES TO DETAIN
		THIS SURPLUTINE REAUS 4040 THE SERIES VALUES AND AVERAGES TO DETAIL
		1024 VALUES FUR MAIN PROGRAM ANALYSIS
	C	MGAGEAGAGF NUMBER
	ç	MONTHEMUNTH OF RECORDING
	÷ Ç	MDAY=DAY DF RECONDING
	C	MTIMENTIME OF RECORDING
10	C	REALMARRAY OF AVERAGED TIME SERIES VALUES
		SUBRUUTINE BUF(MGAGE:MONTH:MDAY:MTIME:REAL:IDATE:END)
		DIMENBIUN CNTL(4096)+IA(5000)
		DIMENSION REAL(1024)
		LUGICAL END
15		00 12 J=1.409h
		CNTL(J)=0.0
	16	CONTINUE
	•	SUFFER IN(9+1)(IA(1)+IA(5000))
		1F(UNIT(9))10-20-30
20	20) PRINT 11.(14(1).181.4)
•••	11	FURMAT((PARITY ERRUN ON (+417)
	10	CUNTINUE
	••	MGGGETA(1)
		MUNTHETA(2)
25		MDAVETACE
.,		MTIMETACA1
3.0		
30		
	26	
	٤.	
	29	
22		
		The set of
- 0	27	OCTINGE
40		REIURN
	30	ENDE TRUE
		RETURN
		END

Figure 7. Listing of BUF subroutine.

V. SAMPLE OUTPUT

Three examples of output are presented for different dates for the wave gage pair at Channel Islands Harbor (Fig. 8). The year the data was taken was 1975.

The first set of frequencies lists amplitude modules squared of wave data having impossible direction results. The sum total of this energy (in decimal percent) is listed as the quantity RSODD in the variable output at the bottom of the output. In the case of the wave data taken on 7-26-1600, the incoherent data amounted to 0.004 (0.4 percent) of the total energy in the wave record.

The second set of frequencies listed provides the wave direction for the frequency bands having a significant part of the energy (≥ 2.5 percent). In the case of the wave record taken on 7-26-1600, it is seen that the wave angle is reasonably consistent from the frequency-to-frequency band and is approximately 0.70 radian (40.1°).

The variable list provided at the bottom of the sampled output gives values of most importance in the analysis of wave information for longshore energy flux. The longshore energy flux output is in pounds per second units; the output in the first example is 89.23 pounds per second.

Example 1

311 7 26 1600 312 7 26 1600 1 316408 000025 4 024544 000014 5 030680 000027 7 042951 000028 9 055223 000014 10 061359 000028 14 065903 0000012 24 147262 000012 25 153390 000004 27 165670 000040 28 17942 000029 29 17942 000029 30 184076 000040 32 196350 000029 42 257709 000041 65 398855 000029 42 25717 04032868 7789305 74 4505511 10395194 6978613 75 44019424 06896760 6919809 75 44019424 06896760 6919809 75 44019424 06896760 6919809 76<	GAUGE NO	. ML	UNTH	DAY	TIME		
312 7 26 1600 1 316#4(1) FMDSQ(1) 3 018408 000025 4 024544 000027 7 004251 000027 10 055223 000012 11 067495 000027 24 147262 000127 25 153398 000002 24 147262 000127 25 153398 000004 27 165570 00002 28 17942 000040 32 196350 000040 33 202465 000024 42 257709 000041 45 27617 000041 45 27617 000041 45 276935 000040 42 257709 000041 45 27617 00032966 73 4492359 02831251 66 41724277 04032966 75 40019424 06590780 76 4766201 0250015 77 48473793 04437262 79 48473793 04437262 80M1= 229 30M2= 80M2	311		7	20	1600		
1 \$16MA(1) FMDBQ(1) 3 .018408 .000025 4 .024544 .000014 5 .030680 .000027 7 .042451 .000021 10 .051559 .000021 11 .067495 .000021 14 .065903 .000027 25 .153398 .000021 27 .165570 .000020 28 .177942 .000041 27 .165570 .000041 27 .165570 .000041 32 .196350 .000041 32 .202485 .000041 45 .27709 .000141 45 .27709 .000141 45 .27709 .000141 45 .27709 .000141 45 .27709 .020121 46 .41724277 .040329861 .7799505 73 .4492359 .0281251 .66337628 75	312		7,	59	1600		
3 018408 000025 4 024544 000014 5 030640 000027 7 042951 000021 10 061359 000021 11 067495 000021 14 005903 000021 14 005903 000021 24 147262 00012 25 153399 000029 24 147762 000040 30 184076 000040 32 196550 000029 42 257709 000040 32 196355 000029 42 257709 000040 33 202485 000029 42 257709 000040 45 378635 000029 42 257709 000041 68 41724277 04032986 7799055 73 4479239 02831251 68437628 74 45065201 0250015 <td>I</td> <td></td> <td>SIGMA(I)</td> <td></td> <td>FMDSQ(I)</td> <td></td> <td></td>	I		SIGMA(I)		FMDSQ(I)		
4 .02454 .000014 5 .030600 .000027 7 .042951 .000012 10 .061359 .000021 11 .067495 .000040 14 .065903 .000040 14 .065903 .000040 24 .147262 .000041 27 .165670 .000040 30 .184076 .000040 32 .196350 .000040 32 .196350 .000040 32 .196350 .000040 32 .196350 .000040 33 .202465 .000041 65 .399835 .000041 65 .399835 .000041 65 .4479239 .0231251 .68437628 74 .45405831 .10359144 .6690760 .69198090 75 .46019424 .06690760 .69198090 .69198090 .71912354 79 .48473793 .04457282 .63791396 .71912354 79 .48473793 .04457282	j		.018408		.000025		
\$.030680 .000037 7 .042951 .000036 9 .055223 .000012 10 .061359 .000021 11 .067495 .000005 24 .147262 .000127 25 .153398 .000041 27 .165670 .000041 28 .177942 .000040 30 .184076 .000041 32 .196350 .000040 32 .196350 .000041 42 .257709 .000041 65 .396835 .000029 42 .257709 .000041 65 .396835 .000029 73 .4479239 .02831251 .88437028 74 .45405631 .03994604 .7799305 73 .44792239 .02831251 .68437028 75 .46019424 .06890760 .69198090 78 .47860201 .02500015 .71912554 79 </td <td>4</td> <td></td> <td>.024544</td> <td></td> <td>.000014</td> <td></td> <td></td>	4		.024544		.000014		
7 .002951 .000036 9 .055223 .000012 10 .061359 .000021 11 .067495 .000046 14 .085903 .00002 24 .447262 .000127 25 .153390 .000041 27 .165670 .000040 30 .184076 .000040 32 .96350 .000040 32 .202485 .000029 42 .257709 .000041 65 .396835 .000041 65 .396835 .000041 65 .396835 .000041 65 .396835 .000041 65 .4479239 .02831251 .68437628 74 .45405831 .1039144 .69736413 75 .46019424 .06809760 .69198090 78 .46019424 .06590760 .69198090 78 .4604937423 .024357282 .63791396 79 .48473793 .04457282 .63791396 8UM1= <	5		.030680		.000027		
9 .055223 .000012 10 .061359 .000021 11 .067495 .000048 14 .065903 .000048 14 .065903 .000048 14 .065903 .000048 14 .065903 .000048 24 .117742 .000041 27 .165670 .000002 29 .177942 .000002 30 .184076 .000029 42 .257709 .000014 45 .276117 .000014 65 .398835 .0000093 1 .91GMA(1) PCT THETA(1) 67 .41110685 .03904604 .70276903 68 .4172277 .04032986 .77993055 73 .4479239 .02031251 .68437628 74 .45405831 .10353194 .69198090 75 .46019424 .06690760 .69198090 78 .47660201 .0250015 .71912354 9041 .2932 .202 .63791396	7		.042951		.000036		
10 001359 000001 11 007495 00000 24 147262 000187 25 153399 00000 27 105670 00000 29 177942 000099 30 104076 000006 33 202445 000029 42 257709 000014 45 276117 000004 65 3398855 0000093 1 81GMA(1) PCT THETA(1) 67 1110685 03904604 70276903 68 1172277 04032988 77993085 73 44702239 0231251 88437628 74 45405851 1039514 66738613 75 46019424 06690760 69198090 78 47860201 02510015 7191254 79 48473793 04457262 653791396 NSALFR# 201 DEPTH OF WATER AT GAUGE SITE# 23.2 AVG1# 21.411 AVG2# 19.909 80H1# 0084 WSUM2# 0086 79 48473793 04457262 653791396 NSALFR# 201 DEPTH OF WATER AT GAUGE SITE# 23.2 AVG1# 21.411 AVG2# 19.909 80H1# 0084 WSUM2# 0086 REATING WAYE HELGHT H## 3.03 BREAKING WAYE HE	9		.055223		.000012		
11 .007495 .000048 14 .005903 .00005 24 .147262 .000127 25 .153390 .000002 27 .165670 .000002 29 .17942 .000040 32 .196350 .000040 32 .196350 .000040 32 .202485 .000040 42 .257709 .000041 65 .398835 .000040 65 .398835 .000041 65 .398835 .000041 65 .398835 .000041 65 .41724277 .04032986 .7799305 73 .4479239 .0281251 .8843728 74 .45405811 .10393144 .69736613 75 .46019424 .06890760 .69798613 75 .464019424 .06890760 .69798613 75 .464019424 .06890760 .69798613 76 .47660201 .02500015 .71912354 79 .48473793 .04457282 .6379	10		.061359		.000021		
14 .003403 .000003 24 .147762 .000127 25 .153398 .000002 27 .165670 .000002 30 .184076 .000002 32 .196350 .000028 42 .257709 .000014 45 .276117 .000014 65 .3798835 .0000093 1 \$IGMA(1) PCT THETA(1) 67 .61110685 .03004604 .70276903 68 .4172277 .04032986 .77995055 73 .4479239 .02631251 .68437628 74 .45905811 .10393194 .66738613 75 .46019424 .06690760 .667198030 78 .47860201 .0250015 .71912554 79 .48473793 .04457282 .63791396 8UM1= .084 %0M2= .234 %SUM1= .084 %0M2= .036 %SUM1= .084 %0M2= .036 %SUM1= .084 %0M2= .036	11		.067495		.000048		
24 .197282 .000127 25 .153399 .000041 27 .165670 .000041 29 .177942 .000099 30 .184076 .000040 32 .196350 .000040 32 .257709 .000014 45 .276117 .000041 65 .398835 .000093 1 .0170279 .00014 65 .398835 .000093 1 .0170276903 66 .41724277 .04032986 73 .4479239 .02031251 .66 .41724277 .04032986 73 .4479239 .02031251 .66 .01709305 73 .4479239 .75 .46019424 .0689760 .69198090 .78 .47860201 .0250015 .79 .48473793 .04457282 .0190 .0250015 .71912354 .99 .024 .0689760 .63791396 .03405782 .63791396 .111 .029 .029 .04457282 .63791396 .04457282 .63791396 .04457282 .63791396	14		.005903		.000005		
27 165570 000002 29 17942 000099 30 184076 000020 32 196350 000020 42 257709 000040 42 257709 000041 65 396835 000020 42 257709 000041 65 396835 000041 65 396835 000041 65 4110665 03904604 .70276903 66 41724277 04032966 .7799505 73 44479239 02831251 .88437028 74 45405631 10393194 .69736613 75 .46019424 06890760 .69736613 75 .46019424 06890760 .69736613 78 .47860201 .02500015 .71912554 79 .48473793 .04457282 .63791396 N8ALFR# 201 0250015 .71912554 79 .48473793 .04457282 .63791396 N8ALFR# 201 0250015 .71912554	24		.151108		.000127		
24 177942 000002 30 184076 000040 32 196350 000066 33 202485 000029 42 257709 000040 45 276117 000041 65 4110655 03904604 .70276903 1 #IGMA(1) PCT THETA(1) 67 41110655 .03904604 .70276903 68 41724277 .04032988 .77995055 73 .44792339 .02631251 .68437628 74 .4505811 .1039144 .66738613 75 .46019424 .06590760 .667198070 78 .46019424 .06590760 .667198070 78 .4647860201 .0250015 .71912554 79 .48473793 .04457282 .63791396 N8ALFR# 201 .0250015 .71912554 79 .48473793 .04457282 .63791396 N8ALFR# 201 .02457282 .63791396 N8ALFR# 201 .0240 .04457282 .	27		165670		000041		
30 .184078 .000040 32 .196350 .000066 33 .202485 .000029 42 .257709 .000041 45 .276117 .000041 65 .398835 .000093 1 \$IGMA(1) PCT THETA(1) 67 .4110685 .03904604 .70276903 68 .41724277 .04032986 .77993085 73 .4479239 .02031251 .88437628 74 .45405311 .1039194 .69738813 75 .46019424 .06890760 .69198090 78 .47860201 .0250015 .71912354 79 .48473793 .04457282 .63791396 NSALFR# 201 .0250015 .71912354 79 .48473793 .04457282 .63791396 NSALFR# 201 .0250015 .71912354 79 .8493938 .038 .63791396 NSALFR# .029 .0497282 .63791396 NSALFR# .029 .04457282 .63791396	29		177942		.000002		
32 .196350 .000066 33 .202485 .000029 42 .257709 .000041 45 .276117 .000041 65 .398835 .000093 1 \$IGMA(1) PCT THETA(1) 67 .4110685 .03904604 .70276903 68 .41724277 .04032988 .77993085 73 .4470239 .02031251 .86437628 74 .45405831 .10395194 .66738613 75 .46019424 .06890760 .69198090 78 .47860201 .02500015 .71912354 79 .48473793 .04457282 .63791396 NSALFR# 201 .02500015 .71912354 79 .48473793 .04457282 .63791396 NSALFR# 201 .0250015 .71912354 NSALFR# 201 .0250015 .71912354 8UM1= .064 .80M2# .234 NSALFR# .229 .04457282 .63791396 SUMEN# .18433938 .03	30		.184078		.000040		
33 .202485 .000020 42 .257709 .000014 45 .276117 .000041 65 .390835 .0000043 1 \$IGMA(I) PCT THETA(I) 67 .4110685 .03904604 .70276903 68 .41724277 .04032986 .77795085 73 .44479239 .02031251 .88437628 74 .45405831 .1039144 .66909760 .669198090 75 .46019424 .06809760 .669198090 .71912354 78 .46473793 .04457282 .63791396 79 .48473793 .04457282 .63791396 8UM1= .064 M6UM2= .04457282 .63791396 8UM1= .064 M6UM2= .084 .04457282 .63791396 8UM1= .064 M6UM2= .045998 .0729 .04457282 .63791396 8UM1= .064 M6UM2= .045998 .0170 .0170 .0170 90000 .0040 R8HFH0= .213 R8LFRW# .0170 <td>32</td> <td></td> <td>.196350</td> <td></td> <td>.000066</td> <td></td> <td></td>	32		.196350		.000066		
42 .357709 .000014 45 .276117 .000041 65 .398835 .000093 1 \$IGMA(1) PCT THETA(1) 67 .4110685 .03904604 .70276903 68 .4172277 .04032986 .77993055 73 .4479239 .02031251 .68437628 74 .45405831 .10393194 .66198070 75 .46019424 .06890760 .66198070 75 .46019424 .06890760 .66198070 75 .46019424 .02500015 .71912354 79 .48473793 .04457282 .63791396 N8ALFR# 201 .04457282 .63791396 N8ALFR# .0040 .847102 .2729 <	33		.202485		.000029		
45 .276117 .000041 65 .398835 .000093 I \$IGMA(1) PCT THETA(1) 67 .41110685 .03904604 .70276903 68 .41724277 .04032888 .77993085 73 .4479239 .02831251 .88437828 74 .458405831 .10395194 .69738613 75 .46019424 .06890760 .69198090 78 .47860201 .0250015 .71912354 79 .48473793 .04457282 .63791396 N8ALFR# 201 DEPTH OF WATER AT GAUGE BITE# 23.2 AVG1# 21.411 AVG# 19.999 8UM1# .229 SUM2# .234 #SUM1# .084 #SUM2# .086 RATIOL# .18433938 GREAKING WAVE ELGRITY C6# 11.18 R80DD# .0040 R8HFR# .2113 R8LFRW# .0170	42		.257709		.000014		
65 .398835 .000093 I \$IGMA(I) PCT TMETA(I) 67 .41110685 .03904604 .70276903 68 .41724277 .04032986 .77095085 73 .44792239 .02031251 .88437628 74 .45405631 .10395194 .66736613 75 .46019424 .06890760 .69196090 78 .47860201 .02500015 .71912554 79 .48473793 .04457282 .63791396 NSALFR# 201 .02500015 .71912554 AvG1# 21.411 AvG2# .04457282 .63791396 NSALFR# 201 .02500015 .71912554 .04457282 .63791396 NSALFR# 201 .04457282 .63791396 .04457282 .63791396 NSALFR# 229 SUM2# .234 .04437282 .63791396 NSUM1# .064 MSUM2# .234 .04437282 .039 SUMEN* .18433936 .039 .039 .039 SUMEN* .18433936 .039 </td <td>45</td> <td></td> <td>.276117</td> <td></td> <td>.000041</td> <td></td> <td></td>	45		.276117		.000041		
I \$IGMA(1) PCT THETA(1) 67 *41110685 .03904604 .70276903 68 *41724277 .04032988 .77993085 73 *4479239 .02031251 .88437928 74 *45405631 .10395194 .69738413 75 *46019424 .06890760 .69198090 78 *47860201 .02500015 .71912354 79 *48473793 .04457282 .63791396 NSALFR# 201 DEPTH OF WATER AT GAUGE BITE# 23.2 AVG1# 21.411 AVG2# 23.2 AVG1# 21.411 AVG2# .234 AVG1# 21.411 AVG2# .234 BUM1# .084 WBUM2# .086 WSUM1# .084 WBUM2# .086 WSUM1# .804 WBUM2# .086 BREAKING WAVE ELEARITY C6# 11.18 RS0D0# .0040 RSMFR0# .2113 RSLFRU# .0170	65		. 398835		.000093		
67 41110685 0304604 .70276003 68 41724277 04032886 .77995085 73 .4479239 .02031251 .88437628 74 .45405831 .10375194 .66738613 75 .46019424 .06689760 .66198070 78 .47660201 .02500015 .71912354 79 .48473793 .04457282 .63791396 NSALFR# 201 .02500015 .71912354 79 .48473793 .04457282 .63791396 NSALFR# 201 .02500015 .71912354 VG1# 2141 AVE2# 19.999 8UM1# .064 NSUM2# .234 #SUM1# .064 NSUM2# .234 #SUM1# .064 NSUM2# .234 #SUM1# .064 NSUM2# .036 #ATIO1# 2*750 RATIU2# 2*729 SUMEN# .18433938 .03 BREAKING WAVE HEIGHT H## 3.03 BREAKING WAVE ELESRITY C6# 11.18 R80DD# .0040 RSHFRG# </td <td>Ţ</td> <td></td> <td>RIGMA(I)</td> <td></td> <td>Ret</td> <td>1454</td> <td></td>	Ţ		RIGMA(I)		Ret	1454	
68 41724277 004032986 77995085 73 44792239 002031251 .88437628 74 +45405631 10393194 .66736613 75 +46019424 .06890760 .69198090 78 +47860201 .02500015 .71912354 79 +48473793 .04457282 .63791396 NSALFR# 201 DEPTH DF WATER AT GAUGE BITE# 23.2 AvG1# 21.411 AvG2# .086 AVG2# .234 WSUM1# .064 WSUM2# .234 WSUM1# .064 WSUM2# .234 WSUM1# .064 WSUM2# .086 RATIO1# 2.729 .040 RATIO2# 2.729 SUMEN* .18433938 .03 .03 .0340 .0170 BREAKING WAVE HEIGHTY H## 3.03 .030 .0040 .0170 PLNOIM .040421 PLNEG# .2413 RSLFRU# .0170 PLNET# 60.2271 PLNE# .54150 .0170 <td>67</td> <td></td> <td>.41110685</td> <td></td> <td>.01904604</td> <td>7087</td> <td>001</td>	67		.41110685		.01904604	7087	001
73 .44792339 .02031251 .08437028 74 .45405831 .10393194 .66738613 75 .46019424 .06899760 .66798090 78 .47860201 .02500015 .71912354 79 .48473793 .04457282 .63791396 N8ALFR# 201 .02500015 .71912354 02437282 .63791396 .63791396 N8ALFR# 201 .04457282 .63791396 N8ALFR# 2.03 .04457282 .63791396 N8ALFR# 2.01 .04457282 .63791396 SUM1= .064 .0402# .040 N8ALFR# .01402# .729 .040 SUMEN* .18433938 .03 .03 BREAKING WAVE CELERITY CB# 11.18 <td>68</td> <td></td> <td>.41724277</td> <td></td> <td>.04032988</td> <td>.7790</td> <td>1085</td>	68		.41724277		.04032988	.7790	1085
74 .45405831 .10393194 .66738413 75 .46019424 .06690760 .69198070 78 .47860201 .02500015 .71912354 79 .48473793 .04457282 .63791396 N8ALFR# 201 .02500015 .71912354 79 .48473793 .04457282 .63791396 N8ALFR# 201 .23.2 .4571028 .23.2 AVG18 21.411 AV628 19.999 .234 9UM18 .229 .23.2 .234 #SUM18 .064 .01028 .2729 9UMEN8 .18433938 .03 .068 0REAKING WAVE HEIGHT H08 3.03 .03 .0400 0REAKING WAVE CELERITY C68 11.18 .0170 PLPO88 .0040 .2413 .0170 PLNEI8 60.2211 .01868 .2413	73		.44792239		.02831251	.8841	1628
75 +46019424 +06890760 +69198090 78 +47860201 +02500015 +71912354 79 +48473793 +04457282 +63791396 NSALFR# 201 DEPTH OF WATER AT GAUGE BITE# 23.2 AVG1# 21+411 AVG2# 19.999 SUM1= +084 HSUM2# +086 RATIOL# 2.729 SUM2# +234 WSUM1= +084 HSUM2# +086 RATIOL# 2.729 SUMEN# +18433938 GREAKING WAVE CELERITY C6# 11+18 RSODD# +0040 RSHFRG# +2413 RSLFRU# +0170 PLNEI# 60,2271	74		.45405831		.10395194	+6973	5613
78 +47860201 .02500015 .71912354 79 .48473793 .04457282 .63791396 NSALFR# 201	75		.46019424		.06899760	+69191	8090
79 .48473793 .04457282 .63791396 N8ALFR# 201 DEPTH OF WATER AT GAUGE BITE# 23.2 AVG1# 21.411 AVG2# 19.999 8UM1# .229 SUM2# .234 WSUM1# .084 WSUM2# .086 RATIO1# 2.729 SUM2# .036 8FEAKING WAVE HEIGHT H0# 3.03 8FEAKING WAVE CELERITY C6# 11.18 RS0DD# .0040 RSHFRG# .2413 RSLFRU# .0170 PLN0I# 60.2271 PLNEG# =5.4150 .0170	78		.47860201		.02500015	+71912	2354
NBALFR# 201 DEPTH OF WATER AT GAUGE BITE# 23.2 AVG1# 21.411 AVG2# 19.999 BUM1# .229 BUM2# .234 WSUM1# .084 WBUM2# .086 RATIO1# 2.730 RATIQ2# 2.729 BUMEN# .18433938 8REAKING WAVE HEIGHT H0# 3.03 BREAKING WAVE CELERITY CB# 11.18 RS0D0# .0040 RB0D0# .0040 RBMFHG# .2413 RSLFRW# .0170 PLNE1# 60.2271 PLNEG# =5.4150 .0170	79		.48473793		.04437282	+6379	396
DEPTH OF WATER AT GAUGE BITEM 23.2 AVG1# 21.411 AVG2# 19.999 SUM1# .229 SUM2# .234 W\$UM1# .084 W6UM2# .086 RATI01# 2.730 RATI02# 2.729 SUMEN# .18433938 GREAKING WAVE HEIGHT HO# 3.03 GREAKING WAVE CELERITY C6# 11.18 R\$000# .0040 R\$MFRG# .2413 R\$LFRU# .0170 PLP08# 44.6421 PLNEG# =5.4150 PLNET# 60.2271	NBALFRE				201		
AVG1# 21.411 AVG2# 19.999 SUM1# .229 SUM2# .230 MSUM1# .084 HSUM2# .086 RATIO1# 2.730 RATIO2# 2.729 SUMEN# .18433938 GREAKING WAVE HEIGHT HO# 3.03 GREAKING WAVE CELERITY CB# 11.18 RSODD# .0040 RSHFHG# .2413 RSLFRW# .0170 PLP08# 94.6421 PLNEG# =5.4150 PLNE1# 60.2271	DEPTH OF	WATER AT	GAUGE 81	TER	23.2		
8UM10 .229 SUM20 .234 WSUM10 .084 WSUM20 .086 RATIO10 2.730 RATIO20 2.729 SUMENE .18433938 BREAKING WAVE HEIGHT HOM 3.03 BREAKING WAVE CELERITY COM 11.18 RSODDm .0040 R3HFRGm .2413 RSLFRUM .0170 PLPOSE 44.6421 PLNEGM =5.4150 PLNEIM 60.2271	AVG1#	21.411	Å	VG2=	19,999		
WSUM1= .084 HSUM2= .086 RATIO1= 2.729 SUMEN= .8433938 BREAKING WAVE HEIGHT HB= 3.03 OREAKING WAVE CELERITY CB= 11.18 RSODD= .0040 RSHFNQ= .2413 RSLFRUP .0170 PLPOB= 44.6421 PLNEG= =5.4150 PLNET= 60.2271	SUMIE	.229	3	UM2=	.234		
HATIUIS 2.730 RATIU28 2.729 SUMENS .18433938 SREAKING WAVE HEIGHT HOS 3.03 BREAKING WAVE CELERITY COS 11.18 RSODDS .0040 RSHFNGS .2413 RSLFRUM .0170 PLP085 94.6421 PLNEGS =5.4150 PLNEIS 60.2271	WSUM1=	.084	W	SUM2=	.086		
307ENS .18433938 GREAKING WAVE HEIGHT HOM 3.03 GREAKING WAVE CELERITY COM 11.18 RSODDA .0040 RSHFHGM .2413 RSLFRUM .0170 PLP085 44.6421 PLNEGS =5.4150 PLNETS 60.2271	HATIO18	2.730	R	#SOIT4	2.729		
OREANING MAVE RELEMITING OREANING MAVE CELEMITY COM 11.18 RSODDm 0040 RSHFRG: 2413 RSLFRG: 0170 PLPOB: 44.6421 PLNEG: 5.4150 PLNET: 60.2271	SUMENE	.1843	3439				
RSODD .0040 RSHFRG .2413 RSLFRG .0170 PLP08 94.6421 PLNEG =5.4150 PLNET 60.2271	APEAKING	HAVE HEL	ERTTY CO-		3.03		
PLP08= 94.6421 PLNEG= =5.4150 PLNEI .0170	READOR	HAVE CEL	ERIT CO		11.18	Del Sour	
PLNETa 80.2271	PLPOSE	Su. 6021		INFRE	-2413	ASLFRUE	.0170
	PLNETE	80.2271		2.02.04	-204120		

Figure 8. Three examples of output for wave gage pair at Channel Islands Harbor.

Tranore +	Exa	amp	16	2 2
-----------	-----	-----	----	-----

GAUGE NO	. MUNTH	DAY	TIME	
311	7	26	1800	
312	7	26	1800	
1	SIGHALL	,	PH080(1)	
1	.000130		.000169	
2	•012272		.000099	
3	.018408		.000007	
2	.030680		.000013	
	.0490.87		.000066	
	.055223		.000164	
10	.061359		.000038	
11	.067495		.000000	
13	.079767		.000168	
14	.085903		• 0 0 0 2 0 1	
15	.092039		.000137	
16	.098175		.000114	
18	•110447		• 000055	
19	.116583		.000061	
23	.141126		.000004	
59	.159534		.000072	
28	.171806		.000008	
30	.184078		•000050	
31	.190214		.000006	
42	.257709		.000028	
58	•355884		.000064	
,	BICHACI	,	Det	THETALIS
	0100411		09545330	10C1A(4)
15		1	0/0/JEEY	*/2203013
73	.4001448		.04043310	+ 0 5 0 0 5 E E /
70		8	0/13141/33	.73484734
· · ·	.4/24600	0	.00231300	*/3444/60
NSALFRE			203	
DEPTH OF	WATER AT GAUGE S	ITE=	24.0	
AVG1	22.246	AV024	20.808	
SUM1 #	.299	8UM24	.293	
WSUM1=	.084	WSUM2=	.078	
RATIOIS	3.579	RATIU2=	3.741	
SUMENE	.31014470			
BHEAKING	HAVE HEIGHT HB=		3.61	
BHEAKING	MAVE CELERITY CO		12.22	
RSODDE	.0048	RSHFRQE	.3742	RELFRUE .0114
PLP08=	125.7135	PLNEG	-25.6734	
PLNET	100.0401			

Figure 8. Three examples of output for wave gage pair at Channel Islands Harbor.--Continued

Example 3

.

GAUGE NU.	munim	UAT	TIME	
311	7	26	2000	9
112	7	26	2000	
216			2000	
-				
1	BIGHALI	,	PMDBU(1)	
1	.006136		.000930	
2	s12272		000397	
3	.018408		.000179	
ù	.024544		.000052	
¥.	.042051		.000013	
<u> </u>	.049087		.000021	
	041007		000001	
10	.001354		.000014	
12	.073631		.000074	
13	.079767		.000085	
17	0104311		.000080	
19	.116583		.000008	
23	.141126		.000011	
12	.196350		.000009	
14	- 208621		.000100	
15	.214757		.000104	
10			.000019	
	257709		00006#	
42			000044	
22	+ \$ 37470		.0001.00	
71	e433631		.001034	
1	SIGMA(1)	PCT	THETALL
NBALFRE			202	
DEPTH OF	WATER AT GAUGE	SITE	23.5	
AVGIE	21.702	AV028	20.287	
AUMAN	.251	BUM28	. 266	
WRITHT	- 071	WAIIMA	081	
DATEDA		DATTOR	1 000	
SUNEN-	3.400	IN TINES	3.277	
SOMENS.	.35101417			
DHEAKING	TAVE HEIGHT HE		3.66	
BREAKING	HAVE CELERITY C	5 #	15.50	
RSODDR	.0095	RSHFHUS	.5675	HATLEHAN .0145
PLPOSE	135.5367	PLNEGR	-40.2297	
PLNETS	95.3070			
	-			

Figure 8. Three examples of output for wave gage pair at Channel Islands Harbor.--Continued

- BRUNO, R.O., et al., "Longshore Sand Transport Study at Channel Islands Harbor, California," TP 81-2, U.S. Army, Corps of Engineers, Coastal Engineering Research Center, Fort Belvoir, Va., Mar. 1981.
- HARRIS, D.L., "Finite Spectrum Analyses of Wave Records," Proceedings of the International Symposium on Ocean Wave Measurement and Analysis, American Society of Civil Engineers, 1974, pp. 107-124 (also Reprint 6-74, U.S. Army, Corps of Engineers, Coastal Engineering Research Center, Fort Belvoir, Va., NTIS A002 114).
- KOMAR, P.D., and GAUGHAN, M.K., "Airy Wave Theory and Breaker Height Prediction," *Proceedings of the 13th Coastal Engineering Conference*, American Society of Civil Engineers, Vol. 1, 1972, pp. 405-418.
- THOMPSON, E.F., "Energy Spectra in Shallow U.S. Coastal Waters," TP 80-2, U.S. Army, Corps of Engineers, Coastal Engineering Research Center, Fort Belvoir, Va., Feb. 1980.
- U.S. ARMY, CORPS OF ENGINEERS, COASTAL ENGINEERING RESEARCH CENTER, *Shore Protection Manual*, 3d ed., Vols. I, II, and III, Stock No. 008-022-00113-1, U.S. Government Printing Office, Washington, D.C., 1977, 1,262 pp.

 Walton, Todd L. Walton, Todd L. Computer algorithm to calculate jongshore energy flux and wave direction from a two pressure sensor array / by road L, walton and Nobert G. DeanFort Beivoir, Va.: U.S. Arruy, Corps of Englueers, Coastal Englueering Research Center; Springfield, Va.: available from NTS, 192. (131) P.: 111; 28 cm(Technical paper / U.S. Oastal Englueers, Coastal Englueering Research Center; No. 82-20. (211) P.: 111; 28 cm(Technical paper / U.S. Oastal Englueers, Coastal Englueering Research Center; no. 82-2 (211) P.: 111; 28 cm(Technical paper / U.S. Oastal Englueering Research Center; no. 82-2 (212) P.: 111; 28 cm(Technical paper / U.S. Oastal Englueering Research Program and designed to accept data In the CERC magnetic-tape forma of record lengths consisting of 4,100 values) is used to analyze avave data and sample outputs for some wave records from a wave gage pressure sensor pair are given. 1. Computer programs. 2. Wave direction measurement. 3. Wave gages to a science for the REC magnetic-tape form a wave gage pressure sensor pair are given. 1. Computer programs. 2. Wave direction measurement. 3. Wave gages to a science form. 1. Computer programs. 2. Wave Girection measurement. 3. Wave gages to a science form. 1. Computer programs. 2. Wave Girection measurement. 3. Wave gages to a science form. 203	 Maiton, Todd L. Gomputer algorithm to calculate longshore energy flux and wave direction from a two pressure sensor array / by Todd L, Waiton and Nobert G. DeanPort Belvoir, Va.: U.S. Arry, Orrys of Engineers, Coastal Engineering Research Center; Springfield, Va.: available [1] p.: 1111.; 12 exa(Technical paper / U.S. Coastal Engineering Research Center; so the sensor sense is a sense of the sens
 Walton, Todd L. Malton, Todd L. Computer sigorithm to calculate longshore energy flux and wave ditection from a two pressure sensor array / by Todd L. Maiton and Robert G. DanFor Relvoir, Va.: 10.5. Arry, Corps of Engineers, coastal Engineering Research Center; Springfield, W.: a validable from MTLS, 1932. Marton MTS, 1942. Marton MTS, 111. M	 Walton, Todd L. Computer Jagorithm to calculate longshore energy flux and wave direction from a two pressure sensor array / by Todd L, Walton and Wobert G. PeanFort Balvoir, Va. : U.S. Army. Orgs of Engineers, Coastal Engineering Research Center ; Springfield, Wa. : available from NTIS, 192. [31] p.: iill.; 28 cm(Technical paper / U.S. Coastal Engineering Research Center ; no. 82-2). Cover title. "August 1982. [31] p.: iill.; 28 cm(Technical paper / U.S. Coastal Engineering Research Center ; no. 82-2). Cover title. "August 1982. [31] p.: analyze word data collected at Channel Islands Barbor, ing Research Frogram (or title for the CERC Longshore Sand Transport Research Program (or title or the CERC Longshore Sand Sand Transport Research Program (or title for the SCE Longshore Sand Sand Transport Research Program (or title or the CERC Longshore Sand Sand Transport Scene data and Sangle outpute for some sage presente sensor pair are given. 1. Computer programs. 2. Wave Sage Presente sensor pair are given. 1. Computer programs. 2. Wave spectra 6. Longshore energy finx. I. Title. II. Ban, Nebert (. 11). Setter: Technical paper (Lossial Engineering Research Center (U.S.)); no. 82-2. (Coastal Engineering Research Center (U.S.)); no. 82-2.

